# Regular article The  $Ti<sub>2</sub>H<sub>2</sub>$  molecule: terminal or bridging hydrogens ?

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Abstract. Density functional calculations carried out for  $Ti<sub>2</sub>H<sub>2</sub>$  show that several structures are thermodynamically stable with respect to  $Ti_2 + H_2$ . The ground state of  $Ti<sub>2</sub>H<sub>2</sub>$  is found to be <sup>3</sup>B<sub>1</sub> and it involves two hydrogen bridges in a nonplanar  $C_{2v}$  arrangement. The <sup>1</sup>A<sub>1</sub> state and other triplet states of the bridging structure are only a few kilocalories per mole above the ground state. The  ${}^{1}\Sigma_{g}^{+}$  state, which corresponds to the Ti analogue of acetylene, is energetically less favored than the bridging structure but it is still bound relative to  $Ti_2 + H_2$ . Results are also presented for the  $Ti<sub>2</sub>H$  molecule. Both bridging and terminal isomers are found to be very stable due to the formation of strong covalent  $Ti-H$ bonds. A comparison of the calculated harmonic vibrational frequencies and IR intensities of  $Ti<sub>2</sub>H<sub>2</sub>$  and  $Ti<sub>2</sub>H$ isomers with the spectra from matrix isolation IR studies on  $Ti_x/H_2$  indicates that these molecules may have been produced in low-temperature reactions.

Key words: Density functional theory  $-Ti<sub>2</sub>H<sub>2</sub>$  –  $Ti<sub>2</sub>H$  – Transition-metal hydrides

### 1 Introduction

We have recently identified two new titanium hydride species – HTi( $C_2H_3$ ) and H<sub>2</sub>Ti( $C_2H_2$ ) – which were formed in the reactions of Ti atoms with ethylene in Ar matrices [1]. The singlet states of these species were characterized as titana-cyclopropenes since their structures were analogous to  $C_3H_4$ . The  $H_2Ti(C_2H_2)$  molecule can formally be derived from  $C_3H_4$  by replacing the  $sp<sup>3</sup>$  carbon atom by a four-valent Ti atom, while in HTi(C<sub>2</sub>H<sub>3</sub>), one of the  $sp^2$  carbons is substituted by Ti (see Fig. 1).

There are a few other examples that indicate a close structural resemblance between simple hydrocarbons and their titana analogues. The titane molecule  $(TiH_4)$ , for example, is known to exist in the gas phase at room temperature [2] and its equilibrium structure is predicted to be tetrahedral [3, 4]. The ground state of  $TiH<sub>2</sub>$  is found to be triplet with a bent equilibrium geometry [5, 6], showing similarity with the  $CH<sub>2</sub>$  radical. The reason for these structural analogies lies in the fact that both Ti and C have four valence electrons and their ground states are associated with similar electron configurations  $(s^2d^2 \text{ and } s^2p^2)$ .

The TiH4 molecule has also been produced in lowtemperature rare-gas matrices and it has been characterized by IR spectroscopy [7, 8]. First, Xiao et al. [7] observed that the photolysis of matrix deposits obtained by trapping thermally vaporized Ti and  $H_2$  gave Ti $H_4$ , as well as  $TiH<sub>2</sub>$ . Chertihin and Andrews [8] later used laser-ablated Ti to react with hydrogen in argon and tried to identify all four members in the  $TiH<sub>x</sub>$  $(x = 1-4)$  series among the reaction products. Both matrix isolation experiments, however, indicated that in addition to  $\text{TiH}_x$  species, titanium hydrides with higher Ti stochiometry were also produced in the reactions. No attempts were made to identify these  $Ti_xH_y$  species, but the existence of broad features in the IR spectra around  $1500 \text{ cm}^{-1}$  [7, 8], 1400 cm<sup>-1</sup> [7] and 1250 cm<sup>-1</sup> [8] suggested that two types of bound hydrogens (terminal and bridging) exist in the  $Ti_xH_y$  molecules [8] and that the geometry of these clusters may not be well defined [7]. These conclusions were indeed supported by recent quantum chemical studies on  $Ti<sub>2</sub>H<sub>8</sub>$  and  $Ti<sub>2</sub>H<sub>6</sub>$  clusters  $[9-11]$ . The results obtained at various post-Hartree-Fock levels for these systems revealed a number of closelying stable isomers which always involved both terminal and bridging hydrogens. Webb and Gordon [9, 11] considered these  $Ti<sub>2</sub>H<sub>2n</sub>$  species as possible reaction products in the matrix isolation experiments and assumed that they were formed by the dimerization of  $TiH<sub>3</sub>$  and  $TiH<sub>4</sub>$ .

The present theoretical work is devoted to the simplest  $Ti<sub>2</sub>H<sub>2n</sub>$  species, the  $Ti<sub>2</sub>H<sub>2</sub>$  molecule, which may be derived from the reaction of  $Ti<sub>2</sub>$  with molecular hydrogen. It is shown that  $Ti<sub>2</sub>H<sub>2</sub>$  may exist in several structural forms, of which one is identified as the titana analogue of the acetylene molecule.



 $H_2Ti(C_2H_2)$  $HTi(C<sub>2</sub>H<sub>3</sub>)$ 

Fig. 1. Structure of the  $H_2Ti(C_2H_2)$  and  $HTi(C_2H_3)$  molecules

#### 2 Computational method

The calculations in this work were carried out within the density functional formalism using the Gaussian94 package [12]. The (14,9,5)/[8,5,3] all-electron basis set of Thomass et al. [13] supplemented with two polarization  $p$  functions  $[14]$  and a diffuse d function [15] was chosen to describe the Ti atom, while a standard TZ2P basis from the 6-311G(2d,2p) set [12] was used for H.

Three frequently used exchange-correlation functionals were chosen to solve the Kohn-Sham equations. Namely, the B3LYP, BLYP and BP86 functionals, where B3LYP is Becke's three parameter hybrid exchange functional [16] combined with the correlation functional of Lee, Yang and Parr (LYP) [17], while in BLYP and BP86, B refers to Becke's 1988 exchange functional [18] and P86 is Perdew's 1986 gradient-corrected correlation functional [19].

The geometries of the systems studied were always fully optimized using the Berny algorithm [20]. The harmonic vibrational frequencies were obtained from analytic energy second derivatives. The stabilities of various forms of  $Ti<sub>2</sub>H<sub>2</sub>$  are given with respect to  $Ti<sub>2</sub> + H<sub>2</sub>$ . The dissociation energies were always corrected for the zero-point-energy contributions determined from BP86 harmonic frequencies.

# 3 Results and discussion

#### 3.1 The  $H_2$ ,  $Ti_2$ , TiH and TiH<sub>4</sub> molecules

First of all, results for the ground states of  $Ti<sub>2</sub>$  and  $H<sub>2</sub>$ are presented. The equilibrium bond lengths and the harmonic vibrational frequencies obtained with the three functionals are listed in Table 1. It is also important to see how these functionals perform for systems involving Ti-H bonds; therefore, in Table 1 results for TiH and TiH4 are also included.

While the equilibrium properties of  $H<sub>2</sub>$  [21] are well reproduced with all functionals, this is not quite true for the Ti2 dimer, which has always been a challenge for quantum chemical calculations  $[22-24]$ . The ground state of Ti<sub>2</sub> is  ${}^{3}\Delta_{g}$  [25] and its equilibrium bond length,  $R_{\rm e}$ , and its equilibrium harmonic vibrational frequency,  $\omega_e$ , are known from resonant two-photon ionization [25] and resonance Raman [26] spectroscopic studies. The  ${}^{3}\Delta_a$  state is predicted to be the ground state at the present levels of density functional theory (DFT). The lowest singlet and quintet states are calculated to be about 9–13 kcal/mol above  ${}^{3}\Delta_g$ , while the  ${}^{7}\sum_{u}$  state is predicted to lie even higher in energy (14–19 kcal/mol above the ground state). Table 1 shows that the B3LYP functional underestimates the equilibrium bond length of the  ${}^3\Delta_g$  state by 0.03 A and overestimates its  $\omega_e$  by about 20%. The bond lengths and harmonic frequencies obtained with the generalized gradient approximation (GGA) functionals (BLYP and BP86) are all closer to the experimental values of 1.942 Å and  $408 \text{ cm}^{-1}$ .

All three functionals predict the  $4\Phi$  state to be the ground state of TiH. The results are fairly stable with respect to the functional applied and they show a slight variation from those of a recent DFT study [27] carried out with a somewhat smaller basis set. The calculated bond lengths are about  $0.03 \text{ Å}$  shorter than the experimental value  $(1.785 \text{ Å} [28])$ . The discrepancy between theory and experiment seems to be more severe for  $\omega_e$ , since all DFT predictions are much higher than the experimental IR absorption at  $1385 \text{ cm}^{-1}$ , which was assigned to TiH by Chertihin and Andrews [8]. It is quite clear that the present DFT methodology, which does not account for near-degeneracy electron correlation, might not be sufficient to give very accurate predictions for the open shell  $6\sigma^2 7\sigma^1 3\pi^1 1\delta^1$  configuration associated with the <sup>4</sup> $\Phi$  state of TiH, but the underestimation of  $R_e$  by 0.03 A certainly does not cause an error of  $200 \text{ cm}^{-1}$  in the harmonic frequency. Moreover, most of the extensive correlated ab initio calculations [29–31] also predict  $\omega_e > 1500 \text{ cm}^{-1}$ . For instance, Bauschlicher's full configuration interaction benchmark calculations [30] gave  $\omega_e$  = 1572 cm<sup>-1</sup>, again far from experiment. These results indicate that the observed  $1385 \text{ cm}^{-1}$  band might not be due to TiH.

No experimental data are available for the TiH bond length in TiH4, but the results obtained with the three functionals are all close to  $1.71$  A, which is equal to the value predicted by the coupled-cluster single-double excitation method [4]. The TiH stretching frequencies are more sensitive to the functional since the B3LYP values for both symmetric and asymmetric TiH stretching vibrations are  $60-70$  cm<sup>-1</sup> higher than those of BLYP and BP86. The latter mode is IR active and it has been observed at 1666 cm<sup> $-1$ </sup> [7] and 1664 cm<sup> $-1$ </sup> [8] in Ar matrices. The BLYP and BP86 predictions for this mode appear to be fairly accurate, whereas B3LYP slightly overestimates the observed value. This trend would be the same if corrections for anharmonicity and matrix effects were considered.<sup>1</sup>

<sup>&</sup>lt;sup>1</sup> This correction altogether is expected to be around  $20-30 \text{ cm}^{-1}$ 



In summary, all three functionals perform reasonably well for the systems presented, except that B3LYP gives slight overestimations for both TiTi and TiH stretching frequencies. For further calculations, all three functionals were used to determine the equlibrium geometries and the relative energies, but for the vibrational analysis of the structures obtained only BP86 calculations were carried out.

## 3.2 The  $Ti<sub>2</sub>H<sub>2</sub>$  molecule: various forms

Given that hydrogen atoms may form terminal and bridging  $Ti-H$  bonds with  $Ti<sub>2</sub>$ , four types of structural isomers are considered for  $Ti<sub>2</sub>H<sub>2</sub>$ . These structures are depicted in Fig. 2. The HTiTiH and  $H_2$ TiTi isomers have only terminal hydrogens and they are the titana analogues of the acetylene molecule and the vinylidene radical. The latter structure, however, could not be located either on the triplet or on the singlet  $Ti<sub>2</sub>H<sub>2</sub>$ potential-energy surfaces. Starting from a number of initial structures corresponding to  $H_2$ TiTi, the geometryoptimization procedure always led to the formation of bridging hydrogens. The Ti(H,H)Ti isomer has two bridging hydrogens, while the Ti(H)TiH structure involves one bridging and one terminal hydrogen. The equilibrium geometries and the dissociation energies of the located structures are given in Tables 2-4.

The ground state  $\binom{1}{2}$  of the HTiTiH molecule is linear and it is thermodynamically stable with respect to the  $\text{Ti}_2(^3\Delta_g) + \text{H}_2(^1\Sigma_g^+)$  dissociation limit (Table 2). The BLYP and BP86 dissociation energies range between 7 and 9 kcal/mol, while B3LYP predicts  $\Delta E = 13.6$  kcal/ mol. The TiTi bond length in HTiTiH hardly differs from that in the ground state of  $Ti<sub>2</sub>$ , and the predicted TiH distances are between those in TiH and  $TiH<sub>4</sub>$ . The triplet states of HTiTiH are calculated to be unstable since the dissociation energies are close to zero.

The singlet-triplet splitting is much smaller for the Ti(H,H)Ti form of Ti<sub>2</sub>H<sub>2</sub> (Table 3). All functionals predict the triplet  ${}^{3}B_1$  state to be the ground state, but the lowest singlet state  $({}^{1}A_{1})$  lies only a few kilocalories per mole above  ${}^{3}B_{1}$ . The dissociation energies for these states are 21–25 kcal/mol (for  ${}^{1}A_{1}$ ) and 23–30 kcal/mol (for



Fig. 2. Possible  $Ti<sub>2</sub>H<sub>2</sub>$  isomers

 ${}^{3}B_{1}$ ), showing that the Ti(H,H)Ti structure is notably more stable than HTiTiH. In both the  ${}^{3}B_1$  and the  ${}^{1}A_1$ states, the T<sub>i</sub>H bond lengths are around  $1.87$  A, which is about  $0.13$  A longer than the terminal bonds. The TiTi distance in  $Ti(H,H)Ti$  is significantly larger than in HTiTiH and it shows a variance for the  ${}^{3}B_{1}$  and  ${}^{1}A_{1}$ states: the distances are about  $0.04-0.05$  Å shorter in the

Table 2. Equilibrium structural parameters and dissociation energies for the HTiTiH structure of  $Ti<sub>2</sub> H<sub>2</sub>$ : bond lengths, R, (A) and the dissociation energies,  $\Delta E$ , (kcal/mol) with respect to  $\text{Ti}_2(^3\Delta_g) + \text{H}_2(^1\Sigma_g^+)$ 

${}^{1}\Sigma_{q}^{+}$ state $(D_{\infty h})$	B3LYP	<b>BLYP</b>	<b>BP86</b>	
R(TiT)	1.915	1.951	1.936	
R(TiH)	1.732	1.744	1.736	
ΔΕ	13.6	7.3	8.4	

Table 3. Equilibrium structural parameters and dissociation energies for the Ti(H,H)Ti structure of Ti<sub>2</sub>H<sub>2</sub>:  $R(A)$ , angles,  $\alpha$ (HXH), in degrees and  $\Delta E$  (kcal/mol) with respect to  $\text{Ti}_2(^3\Delta_g) + \text{H}_2(^1\Sigma_g^+)$ .<br>X in  $\alpha$ (HXH) denotes the midpoint of the Ti—Ti bond

	<b>B3LYP</b>	<b>BLYP</b>	<b>BP86</b>	
$^1$ A <sub>1</sub> state $(C_{2v})$				
R(TiT)	2.010	2.044	2.029	
R(TiH)	1.871	1.876	1.866	
$\alpha$ (HXH)	91.4	91.6	91.3	
ΛE	20.9	21.8	25.4	
${}^3B_1$ state $(C_{2v})$				
R(TiT)	2.049	2.089	2.074	
R(TiH)	1.873	1.877	1.865	
$\alpha$ (HXH)	124.1	124.6	125.5	
ΛE	23.2	25.2	29.5	

Table 4. Equilibrium structural parameters and dissociation energies for the HTi(H)Ti structure of Ti<sub>2</sub>H<sub>2</sub>: R (Å),  $\alpha$ (HXH) in degrees and  $\Delta E$  (kcal/mol) with respect to  $\text{Ti}_2(^3\Delta_g) + \text{H}_2(^1\Sigma_g^+)$ .  $R_1$  refers to terminal,  $R_2$  and  $R'_2$  to bridging Ti-H bonds  $(R'_2$  is associated with Ti that binds the terminal hydrogen  $(H<sup>t</sup>)$ )



<sup>a</sup> Geometry optimization carried out with the B3LYP functional for the <sup>3</sup>A' state converges to the Ti(H,H)Ti form

 $b$ <sup>b</sup>The negative sign indicates that HTi(H)Ti is predicted to be unstable

singlet state. Surprisingly, the Ti(H,H)Ti molecule is not planar. The  $D_{2h}$  arrangement of the bridging hydrogens is a transition state on the potential-energy hypersurface. The two TiHTi planes in the equilibrium structure of the  ${}^{1}A_{1}$  state meet at about a right angle,  $\alpha$ (HXH) $\approx$  90°, while this angle is about  $125^{\circ}$  for the ground state. This structure is very similar to that found for the dibridged

Table 5. Dissociation energies (kcal/mol) of various forms of  $Ti<sub>2</sub>H<sub>2</sub>$ 

	<b>B3LYP</b>	<b>BLYP</b>	<b>BP86</b>	
<b>HTiTiH</b> ${}^{1}\Sigma_{g}^{+}$	13.6	7.3	8.4	
Ti(H,H)Ti $A_1$ $3B_1$	20.9 23.2	21.8 25.2	25.4 29.5	
HTi(H)Ti $\mathbf{A}'$ 3A'	$-8.4$	8.2 13.8	10.4 16.3	

disilyne,  $Si(H<sub>2</sub>)Si$ , molecule [32]. It should be mentioned here that a few other triplet states are predicted to lie close to the  ${}^{3}B_1$  state. For instance, BP86 calculations predict the  ${}^{3}A_1$  state to be 4 kcal/mol above the <sup>3</sup>B<sub>1</sub> state with  $R(Ti) = 1.953 \text{ Å}, R(TiH) = 1.884 \text{ Å}$  and  $\alpha(HXH) = 108.4^{\circ}$  equilibrium parameters.

For the Ti(H)TiH isomer, the B3LYP and the GGA results are quite different (Table 4). While the BLYP and BP86 dissociation energies for the  ${}^{1}A'$  and  ${}^{3}A'$  states are calculated to be between those of HTiTiH and Ti(H,H)Ti, the B3LYP functional predicts this form to be unstable with respect to  $Ti_2 + H_2$ . From the B3LYP results, the  ${}^{1}A'$  state is 8 kcal/mol above the dissociation limit, and for the  ${}^{3}A'$  state, B3LYP does not even yield an energy minimum since the geometry optimization converges to the Ti(H,H)Ti structure. The normal coordinate analysis of the vibrational modes carried out at the BLYP and BP86 levels for the located  ${}^{3}A'$  minima shows that both in-plane and out-of-plane  $TiTiH<sup>t</sup>$ bending frequencies are rather low (about  $200 \text{ cm}^{-1}$ ). It appears then that the discrepancy between the B3LYP and GGA results for the  ${}^{3}A'$  state originates in the flat character of the potential-energy surface in the region. All located Ti(H)TiH structures are planar with nearly linear TiTiH<sup>t</sup> parts for the singlet and with  $\alpha$ (TiTiH<sup>t</sup>)  $\approx$  $160^{\circ}$  for the  ${}^{3}\text{\AA}{}'$  state.

The dissociation energies of the located forms of  $Ti<sub>2</sub>H<sub>2</sub>$  are collected in Table 5. They clearly show that the Ti(H,H)Ti structure is energetically favored over the HTiTiH and Ti(H)TiH isomers, with a slight preference for the triplet state. The other two structures are notably less stable, but they are generally bound with respect to  $Ti<sub>2</sub> + H<sub>2</sub>$ . Although the <sup>3</sup>A' state of Ti(H)TiH is found to be lower in energy than the  ${}^{1}A'$  state, the existence of the triplet Ti(H)TiH structure is uncertain. Even if it is a minimum on the triplet surface, it may convert easily to the dibridging form.

Before we proceed to analyze the nature of the bonding in the located  $Ti<sub>2</sub>H<sub>2</sub>$  isomers, the interaction of a single H atom with the ground state of  $Ti<sub>2</sub>$  will be discussed.

#### 3.3 The  $Ti<sub>2</sub>H$  molecule: structure and bonding

A single H atom is able to bind in both end-on and sideon ways to Ti2, resulting in linear TiTiH and bridging Ti(H)Ti molecules. The ground states of these forms are predicted to be  ${}^{2}\Delta$  and  ${}^{4}B_1$ , respectively. While the quartet states of TiTiH are well separated from the ground state, the doublet states of Ti(H)Ti, of which  ${}^{2}B_{1}$ is the lowest, lie very close to  ${}^{4}B_{1}$ . The calculated properties for the  ${}^{2}\Delta$ ,  ${}^{4}B_1$  and  ${}^{2}B_1$  states of Ti<sub>2</sub>H are presented in Table 6.

All functionals predict the  ${}^{4}B_1$  state to be the most stable state followed by the  ${}^{2}B_{1}$  and  ${}^{2}\Delta$  states. The binding energy of the H atom in  ${}^{4}B_1$  is between 60 and 66 kcal/mol, but it is also close to 60 kcal/mol in the TiTiH  $(^{2}\Delta)$  molecule, showing that both terminal and bridging hydrogens are strongly bound to  $Ti<sub>2</sub>$ . For the terminal Ti-H bond,  $R(TiH)=1.74$  A, while the bridging bonds are roughly  $0.1$  A longer. The metalmetal bond becomes shorter in TiTiH and lengthens in Ti(H)Ti compared to that in Ti<sub>2</sub> ( ${}^{3}\Delta_{g}$ ). Consequently, the TiTi stretching vibrational frequency shifts to a higher value in TiTiH and the frequencies are lower in the  ${}^{4}B_1$  and  ${}^{2}B_1$  states of Ti(H)Ti than in Ti<sub>2</sub>. The terminal TiH stretching frequency is predicted to be between 1520 and 1560 cm<sup>-1</sup>, while the symmetric TiH stretching modes in the Ti(H)Ti states are around  $1400 \text{ cm}^{-1}$ . The calculated asymmetric TiH stretching frequencies are around  $1000 \text{ cm}^{-1}$  in  ${}^{4}B_{1}$  and a bit higher (about 1100 cm<sup>-1</sup>) in <sup>2</sup>B<sub>1</sub> states.

To describe the bonding in TiTiH and Ti(H)Ti, let us first recall that the  ${}^3\Delta_q$  state of Ti<sub>2</sub> is associated with the  $1\sigma_g^2 \pi_u^4 2\sigma_g^1 \delta^1$  configuration of valence electrons [23]. Here, the fully occupied  $1\sigma_g$  and  $\pi_u$  orbitals represent 4s-4s and  $3d_{\pi}$ -3d<sub> $\pi$ </sub> bonding overlaps, whereas the singly occupied  $2\sigma_g$  and  $\delta$  are  $3d_{\sigma}$ -3d<sub> $\sigma$ </sub> and  $3d_{\delta}$ -3d<sub> $\delta$ </sub> bonding overlaps (Fig. 3). All these two- and one-electron combinations give rise to a quadruple metal–metal bond in Ti<sub>2</sub>( ${}^{3} \Delta_g$ ).

Table 6. Structural parameters, dissociation energies and IR spectra of various states of Ti<sub>2</sub>H: R (A),  $\Delta E$  (kcal/mol) with respect to Ti<sub>2</sub>( ${}^{3}\Delta_g$ ) + H( ${}^{2}$ S), harmonic frequencies,  $\omega_i$  (cm<sup>-1</sup>) and IR intensities in parentheses) (km/mol)

	B3LYP	<b>BLYP</b>	<b>BP86</b>
TiTiH $(^{2}\Delta)$			
R(TiTi)	1.862	1.895	1.875
R(TiH)	1.736	1.745	1.738
$\Delta E$	56.4	54.3	56.2
$\omega_1(\sigma)$	1563 (594)	1527 (445)	1536 (445)
$\omega_2(\sigma)$	574 (89)	531 (71)	559 (76)
$\omega_3(\pi)$	478 (72)	473 (53)	482 (54)
$Ti(H)Ti ({}^2B_1)$			
R(TiT)	2.039	2.058	2.042
R(TiH)	1.831	1.846	1.832
ΛE	59.3	58.2	63.0
$\omega_1(a_1)$	1434 (49)	1368 (53)	1409 (46)
$\omega_2(b_2)$	1159(41)	1086(23)	1146 (47)
$\omega_3(a_1)$	464(3)	390(3)	388 (3)
$Ti(H)Ti$ $(^4B_1)$			
R(TiT)	1.971	2.029	1.991
R(TiH)	1.850	1.854	1.845
$\Delta E$	60.2	61.6	65.8
$\omega_1(a_1)$	1417(60)	1373 (56)	1397 (56)
$\omega_2(b_2)$	1083(152)	1010(27)	1039 (32)
$\omega_3(a_1)$	397(6)	343(2)	355(3)

The <sup>2</sup> $\Delta$ , <sup>4</sup> $B_1$  and <sup>2</sup> $B_1$  states of Ti<sub>2</sub>H can be derived from the ground states of  $Ti<sub>2</sub>$  and H since all three states dissociate into  $\text{Ti}_2(\textsuperscript{3}\Delta_g) + \text{H}(\textsuperscript{2}\text{S})$ . The dissociation energy curves, derived at the BP86 level by varying the  $Ti-H$ distances with fixed  $R(TiTi)$  values, are depicted in Fig. 4. The analysis of the Kohn–Sham orbitals of various TiTiH and Ti(H)Ti structures along the dissociation curves reveals the bonding mechanisms in the two forms. The singlet pairing of the hydrogen 1s and Ti<sub>2</sub>  $2\sigma_q$ electrons gives rise to a covalent  $Ti-H$  bond in  $TiTH$  $(^{2}\Delta)$ . The doubly occupied  $\sigma$  Ti-H bonding orbital (Fig. 5) has about  $60\%$  1s(H) character, indicating a slight charge transfer from  $Ti<sub>2</sub>$  to H. This orbital is the lowest lying TiTiH valence orbital and is well separated from the pure Ti<sub>2</sub> ( $1\sigma_g$ ,  $\pi_u$  and  $\delta$ ) orbitals. The mixing of 1s(H) with the unpaired Ti<sub>2</sub>2 $\sigma<sub>g</sub>$  and  $\delta$  orbitals is unfavored in the Ti(H)Ti isomer, but  $1s(H)$  can interact with the more diffuse and doubly occupied  $1\sigma_q$  orbital. To decrease the two-orbital three-electron repulsive interaction between the occupied orbitals (Pauli repulsion), the metal 4s electrons polarize away from H through mixing of  $1\sigma_a$  with the in-plane component of  $\pi_u$  and, on the other hand, 4s electrons are excited to an empty metal orbital. The excitation can take place either in the majority or in the minority spin orbital space leading to the  ${}^{4}B_1$  and  ${}^{2}B_1$  states, respectively. In their equilibrium structures, the Ti-H bonding orbitals of  ${}^{4}B_1$  and  ${}^{2}B_1$  are the lowest-lying valence orbitals, which are doubly occupied three-center  $a_1$  orbitals, again having 60% 1s(H)

and 40% Ti<sub>2</sub> ( $1\sigma_g + \pi_u$ ) character (Fig. 5).<br>We see that the terminal and the bridging Ti-H bonds in the two forms of T<sub>i2</sub>H are strong covalent bonds with slight ionic character. The formation of these bonds, however, has a different influence on the strength of the Ti-Ti bond. Since the Ti 4s and  $3d_{\pi}$ electrons become involved in the  $Ti-H$  bonds in  $Ti(H)Ti$ , the metal-metal interaction is weakened with respect to that in  $\text{Ti}_2(^3\Delta_g)$ . Although the  $\sigma(\text{Ti-H})$ bonding orbital in TiTiH has a nonnegligible Ti 4s admixture, the  $3d_{\pi}$ -3d<sub> $\pi$ </sub> bond is unaffected in this form.

## 3.4 Bonding in HTiTiH and  $Ti(H,H)$ Ti

The TiTiH  $(^{2}\Delta)$  molecule can bind a second H atom on the other side of the  $Ti<sub>2</sub>$  without loosening the 4s-4s and  $3d_{\pi}$ -3d<sub> $_{\pi}$ </sub> metal–metal bonds. Although the  $3d_{\sigma}$ -3d<sub> $_{\sigma}$ </sub> is weakened because the  $\sigma_u$  combination of the two Ti-H overlaps is Ti-Ti antibonding (Fig. 6), the Ti<sub>2</sub>  $1\sigma_q(4s)$ and  $\pi_u(3d_\pi)$  orbitals are practically unchanged when going from  $\text{Ti}_2(^3\Delta_g)$  to  $\text{HTITH}(\text{I}_{\Sigma_g}^+)$ . This type of bonding is analogous to that in acetylene in that both molecules have strong covalent  $X-H$  bonds and the heavy atoms are linked through a triple bond. The main difference between the highest occupied molecular orbital and the lowest unoccupied molecular orbital is that the  $\pi$  components of the Ti  $\equiv$  Ti bond are due to  $d$ -type orbitals, while they are a result of  $p$ - $p$  overlaps in  $C_2H_2$ . For this reason, the energy difference between the highest occupied molecular orbital and the lowest unoccupied molecular orbital is much smaller in HTiTiH (around 0.7 eV versus around 7 eV in  $C_2H_2$ ), but it is

Fig. 3. Valence orbitals of Ti<sub>2</sub> $(3\Delta_a)$ . (Plotted with the Molekel visualization program [33])





 $2\sigma_{\rm g}(3{\rm d}_{\rm o})$ 

 $\delta(3d_{\delta})$ 





 $1\sigma_{\rm g}(4{\rm s})$ 

 $\pi_{\mathfrak{m}}(3d_{\pi})$ 





still sufficient to separate the singlet ground state from the triplets. The existence of the triple bond between the Ti atoms is unambiguously confirmed by calculating the Mayer bond orders  $[34-36]$ . For the Ti-Ti overlap, the Mayer bond order is very close to 3.0 and is independent of the functional applied.

The Ti-Ti bond is much weaker in the Ti $(H,H)$ Ti molecule, since due to the nonplanar arrangement of the H atoms both  $\pi_u(3d_\pi)$  components of Ti<sub>2</sub> contribute to the Ti-H bonds (Fig. 7). In the planar Ti $(H,H)$ Ti structure, the symmetric  $(++)$  combination of 1s(H) orbitals does not overlap with the in-plane  $\pi_u(3d_\pi)$  Ti<sub>2</sub> orbital for symmetry reasons, so this structure is energetically less favored. The  $1s(H) - \pi_u(3d_\pi)$  (Ti<sub>2</sub>) overlap is maximized at  $\alpha(HXH) = 90^{\circ}$ , which is apparent in the equilibrium structure of the  ${}^{1}A_{1}$  state. In the ground state  $({}^3B_1)$  of Ti(H,H)Ti, the presence of a singly occupied  $a_1$  orbital, which is a Ti<sub>2</sub>  $\delta(3d_{\delta})$  orbital (Fig. 3), pushes apart the hydrogen atoms due to Pauli repulsion. Consequently, the  $\alpha(HXH)$  angle in the <sup>3</sup>B<sub>1</sub> state is an obtuse angle (around 125°).

The Ti-Ti bond would undergo further weakening if additional H atoms were attached to  $Ti<sub>2</sub>H<sub>2</sub>$ . Preliminary results for  $Ti<sub>2</sub>H<sub>4</sub>$  indicate considerable metal-metal overlaps in both double and quadruple hydrogenbridged structures [HTi(H,H)TiH and Ti(H,H,H,H)Ti in our notation], but as shown by Webb and Gordon [9, 11], there is only little or no direct bonding between the



 $\sigma$ (Ti-H)  $a_i$ (Ti-H)

Fig. 5. Ti-H bonding orbitals of TiTiH  $[\sigma(Ti-H)]$  and Ti(H)Ti  $[a_1(Ti-H)]$ 



 $\sigma_{g}$ (Ti-H)

Fig. 6. Ti-H bonding orbitals of HTiTiH



$a_i$ (Ti-H)	$\mathsf{b}_1$

Fig. 7. Ti-H bonding orbitals of Ti $(H,H)$ Ti

Table 7. Binding energies (kcal/mol) of the first and the second H atom in Ti<sub>2</sub>H<sub>2</sub>

 $(Ti-H)$ 



titanium atoms in the located  $Ti<sub>2</sub>H<sub>6</sub>$  and  $Ti<sub>2</sub>H<sub>8</sub>$  structures  $[R(TiTi)]$  is between 2.5 and 3.1 A in these clusters].<sup>2</sup>

We saw in the previous section that the formation of the bridging Ti-H bonds in  $Ti<sub>2</sub>H$  is slightly preferred over the terminal linkage. This is also the case for the binding of the second H atom. Table 7, where the binding energies of the first and the second hydrogen for the terminal and bridging structures are collected, shows that the energy of the Ti(H)Ti + H  $\rightarrow$  Ti(H,H)Ti reaction is  $6-11$  kcal/mol larger than the energy of the TiTiH +  $H \rightarrow H$ TiTiH reaction, providing an explanation for the enhanced stability of the Ti(H,H)Ti structure compared to HTiTiH.

## 3.5 Vibrational analysis for HTiTiH and  $Ti(H,H)$ Ti

The predicted harmonic vibrational frequencies and IR intensities of the HTiTiH and Ti(H,H)Ti forms of  $Ti<sub>2</sub>H<sub>2</sub>$ are given in Table 8. Assuming that the BP86 functional gives reasonable frequencies for TiH stretching frequencies, the possibility of the existence of  $Ti<sub>2</sub>H<sub>2</sub>$  among the matrix-isolated  $Ti_xH_y$  products is examined in this section.

From the two TiH stretching modes of HTiTiH, only the asymmetric combination  $(\sigma_u)$  is IR active. This band is predicted to be a rather intense absorption above  $1500 \text{ cm}^{-1}$ . If the HTiTiH molecule is isolated in raregas matrices then it is expected to give a sharp TiH stretching band since its geometry and its ground state are well defined (the molecule is not floppy and has no low-lying states). In the matrix study reported by Xiao et al. [7], a sharp band at  $1512 \text{ cm}^{-1}$  was observed when small titanium clusters were codeposited with molecular hydrogen. This band disappeared after the matrix was photolyzed with UV light. The calculated  $\omega_2(\sigma_u) = 1548$  cm<sup>-1</sup> is reasonably close to the observed frequency and the calculated  $HTiTH \rightarrow DTiTD$  isotopic shift for this mode  $(H/D = 1.399)$  is also consistent with the experimental shift  $(H/D = 1.387)$ . In the laserablation matrix study [8], several IR bands were observed around  $1500 \text{ cm}^{-1}$  and they were associated with  $Ti_xH_y$  species. Of these bands, the sharp absorption at  $1485 \text{ cm}^{-1}$  and its corresponding Ti/D<sub>2</sub> band at  $1071$  cm<sup>-1</sup> did not shift when the reaction was made with mixed hydrogen (HD). On the basis of this observation, the authors suggested that the  $1485 \text{ cm}^{-1}$  band belongs either to a species involving a single H atom or to a molecule with two uncoupled hydrogens. The present calculations indicate that the motion of the two hydrogens in HTiTiH is coupled. The two TiH stretching modes are split by  $31 \text{ cm}^{-1}$  (Table 8); in line with this, the TiH stretching and TiD stretching frequencies of HTiTiD undergo notable shifts with respect to those

<sup>2</sup> B3LYP calculations with the present basis set predict that on the singlet potential-energy surface the quadruple-bridging  $Ti<sub>2</sub>H<sub>4</sub>$ structure is 14 kcal/mol below the double-bridging form, and in both structures the TiTi bond length is around  $2.1 \text{ Å}$ . The titana analogue of the ethylene molecule  $(H_2TiTH_2)$  is predicted to be a transition state far above the quadruple-bridging structure

Table 8. IR spectra of HTiTiH, Ti(H,H)Ti and their deuterated forms calculated using the BP86 functional: harmonic frequencies  $(cm<sup>-1</sup>)$ , IR intensities in *parentheses* (km/mol). The symmetry and the approximate description are given for each normal mode of the

 $Ti<sub>2</sub>H<sub>2</sub>$  forms. For the Ti(H,H)Ti molecule, the displacement of the H atoms in the  $b_1$  TiH stretching mode is along the HXH plane, whereas the H atoms move parallel to the TiXTi plane in the  $b_2$ TiH stretching mode  $(X$  denotes the midpoint of  $Ti<sub>2</sub>$ )

		Ti <sub>2</sub> H <sub>2</sub>	Ti <sub>2</sub> HD	Ti <sub>2</sub> D <sub>2</sub>
HTiTiH $(^1A_{1a})$				
$\omega_1(\sigma_a)$	Symmetric TiH stretch	1579(0)	1513 (335)	1128(0)
$\omega_2(\sigma_u)$	Asymmetric TiH stretch	1548 (796)	1117 (220)	1106 (407)
$\omega_3(\pi_a)$	Asymmetric TiTiH bend	556 (0)	493 (23)	420(0)
$\omega_4(\sigma_q)$	TiTi stretch	533 $(0)$	530 $(0)$	528 (0)
$\omega_5(\pi_u)$	Symmetric TiTiH bend	336 (211)	271 (130)	240 (108)
$Ti(H,H)Ti~(^1A_1)$				
$\omega_1(a_1)$	TiH stretch	1383 (152)	1370 (126)	988 (73)
$\omega_2(b_1)$	TiH stretch	1356 (101)	976 (62)	964 (51)
$\omega_3(b_2)$	TiH stretch	1004(12)	967(7)	725(7)
$\omega_4(a_2)$	TiH stretch	921(0)	669(2)	659 (0)
$\omega_5(a_1)$	HXH bend	668 (1)	581 (2)	475 (1)
$\omega_6(a_1)$	TiTi stretch	463(9)	462 (9)	461 (9)
$Ti(H,H)Ti ({}^3B_1)$				
$\omega_1(a_1)$	TiH stretch	1374 (61)	1371 (85)	979 (30)
$\omega_2(b_1)$	TiH stretch	1369 (111)	977 (43)	976 (56)
$\omega_3(b_2)$	TiH stretch	1016(11)	996 (6)	730 (6)
$\omega_4(a_2)$	TiH stretch	973(0)	714 (2)	701(0)
$\omega_5(a_1)$	TiTi stretch	433(6)	432 (6)	431 $(5)$
$\omega_6(a_1)$	HXH bend	344 (18)	298 (14)	245(9)

in HTiTiH and DTiTiD. For this reason, the assignment of the  $1485 \text{ cm}^{-1}$  band to HTiTiH can probably be ruled out, but this band may belong to  $TiTiH(^2\Delta)$ , for which we get  $\omega_1(\sigma) = 1536 \text{ cm}^{-1}$  at the BP86 level (Table 6) with the corresponding TiTiD( ${}^{2}\Delta$ ) prediction of  $\omega_1(\sigma) =$  $1097$  cm<sup>-1</sup>.

The  $a_1$  and  $b_1$  TiH stretching frequencies of the bridging  $Ti<sub>2</sub>H<sub>2</sub>$  molecule are predicted to be less intense than  $\omega_2(\sigma_u)$  of HTiTiH, but they should still be quite strong absorptions in the 1350–1400 cm<sup>-1</sup> region. The  $a_1$ and  $b_1$  combinations split up by only a few wavenumbers in the ground state of Ti(H,H)Ti and by almost 30  $cm^{-1}$ in the  ${}^{1}A_1$  state. With high Ti concentration, Xiao et al. observed a broad feature in this part of the IR spectra with a sharp band at 1396  $cm^{-1}$ , which disappeared after UV photolysis. This latter band or/and other bands in the broad feature could be due to Ti(H,H)Ti. The 1350-1400 cm<sup>-1</sup> region is rather simple in the spectra of Chertihin and Andrews [8]. Only a doublet at 1385/ 1389 cm<sup>-1</sup> was observed; the intensity of the 1385 cm<sup>-1</sup> peak depended strongly on the laser power. The 1389 cm<sup>-1</sup> band was assigned to  $HO_2$  and from a comparison with Hartree–Fock calculations the  $1385$  cm<sup>-1</sup> band was associated with the TiH dimer. As noted before, both high-quality ab initio and DFT calculations give much higher frequencies for the ground state of TiH. If this band is not due to TiH then it may belong to another  $Ti_xH$  species with  $x > 1$  because its isotopic behavior is consistent with a product with a single H atom. Any of the  ${}^{4}B_1$  and  ${}^{2}B_1$  states of Ti(H)Ti would be a good candidate for this species since their predicted  $a_1$  TiH stretching frequencies match well with the observed frequency. In this case, however, one should observe another band either around  $1000 \text{ cm}^{-1}$  $({}^4B_1$  state) or around 1100 cm<sup>-1</sup>  $({}^2B_1$  state) with a comparable intensity as the 1385 cm<sup>-1</sup> peak (Table 6). Some bands are indeed listed in Table I of Ref. [8], but they were associated with  $HO<sub>2</sub>$  and TiO species.

#### 4 Summary and concluding remarks

Although the HTiTiH isomer of  $Ti<sub>2</sub>H<sub>2</sub>$  with two terminal hydrogens and the triple metal-metal bond is found to be thermodynamically stable with respect to  $Ti<sub>2</sub> + H<sub>2</sub>$ , this structure does not represent the global minimum on the  $Ti<sub>2</sub>H<sub>2</sub>$  potential-energy surfaces. In spite of the similarity of the valence electron shells of Ti and C atoms, the first two hydrogens prefer to bind to  $Ti<sub>2</sub>$  in the bridging position. That is why the bridging Ti(H,H)Ti isomer is notably more stable than the HTiTiH form. For more saturated  $Ti<sub>2</sub>H<sub>2n</sub>$  species  $(n = 2 \text{ and } 3)$ , the titana-hydrocarbon structures  $(H_2T_1)$ - $TiH<sub>2</sub>$  and  $H<sub>3</sub>TiTiH<sub>3</sub>$ ) do not seem to be stable [9].

A comparison of the predicted IR spectra with those recorded in the  $Ti_x/H_2$  matrix isolation studies provides an indication that both HTiTiH and Ti(H,H)Ti species might have been formed in low-temperature experiments; however, it is quite clear from the discussion presented in Sect 3.5 that at present it is impossible to give definite assignments for the observed bands. All the statements there should be considered as only probability statements. Further careful experimental and theoretical work is required to be able to identify, if they can be at all, the  $Ti<sub>2</sub>H$  and  $Ti<sub>2</sub>H<sub>2</sub>$  species.

Finally, it should be pointed out that the present work was not meant to provide accurate energetic and structural properties for  $Ti<sub>2</sub>H<sub>2</sub>$ . Although no sign of multireference problems (symmetry breaking, unusual harmonic frequencies, spin contamination) was encountered for the molecules investigated, it is quite likely that nondynamic electron correlation contributions should be taken into account to obtain reliable predictions. The present results, however, may serve as a starting point for more demanding calculations.

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